# Computer Architecture: SIMD and GPUs (Part I) 

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## A Note on This Lecture

- These slides are partly from 18-447 Spring 2013, Computer Architecture, Lecture 15: Dataflow and SIMD
- Video of full lecture from 447:
- http://www.youtube.com/watch?v=f-XL4BNRoBA
- Video of the part related to only SIMD and GPUs:
- https://youtube.googleapis.com/v/f-XL4BNRoBA\%26start=4980


## Vector Processing:

Exploiting Regular (Data) Parallelism

## Flynn's Taxonomy of Computers

- Mike Flynn, "Very High-Speed Computing Systems," Proc. of IEEE, 1966
- SISD: Single instruction operates on single data element
- SIMD: Single instruction operates on multiple data elements
- Array processor
- Vector processor
- MISD: Multiple instructions operate on single data element
- Closest form: systolic array processor, streaming processor
- MIMD: Multiple instructions operate on multiple data elements (multiple instruction streams)
- Multiprocessor
- Multithreaded processor


## Data Parallelism

- Concurrency arises from performing the same operations on different pieces of data
- Single instruction multiple data (SIMD)
- E.g., dot product of two vectors
- Contrast with data flow
- Concurrency arises from executing different operations in parallel (in a data driven manner)
- Contrast with thread ("control") parallelism
- Concurrency arises from executing different threads of control in parallel
- SIMD exploits instruction-level parallelism
- Multiple instructions concurrent: instructions happen to be the same


## SIMD Processing

- Single instruction operates on multiple data elements
- In time or in space
- Multiple processing elements
- Time-space duality
- Array processor: Instruction operates on multiple data elements at the same time
- Vector processor: Instruction operates on multiple data elements in consecutive time steps


## Array vs. Vector Processors



Instruction Stream
LD $\quad \mathrm{VR} \leftarrow \mathrm{A}[3: 0]$ ADD VR $\leftarrow \mathrm{VR}, 1$ MUL VR $\leftarrow V R, 2$ ST $\quad \mathrm{A}[3: 0] \leftarrow \mathrm{VR}$

Same op @ same time

| LD0 | LD1 | LD2 | LD3 |
| :--- | :--- | :--- | :--- |
| AD0 | AD1 | AD2 | AD3 |
| MU0 | MU1 | MU2 | MU3 |
| ST0 | ST1 | ST2 | ST3 |

Different ops @ same space



VECTOR PROCESSOR


Same op @ space ST3


## SIMD Array Processing vs. VLIW

- VLIW



## SIMD Array Processing vs. VLIW

- Array processor



## Vector Processors

- A vector is a one-dimensional array of numbers
- Many scientific/commercial programs use vectors

$$
\begin{aligned}
& \text { for }(\mathrm{i}=0 ; i<=49 ; i++) \\
& C[i]=(A[i]+B[i]) / 2
\end{aligned}
$$

- A vector processor is one whose instructions operate on vectors rather than scalar (single data) values
- Basic requirements
- Need to load/store vectors $\rightarrow$ vector registers (contain vectors)
- Need to operate on vectors of different lengths $\rightarrow$ vector length register (VLEN)
- Elements of a vector might be stored apart from each other in memory $\rightarrow$ vector stride register (VSTR)
- Stride: distance between two elements of a vector


## Vector Processors (II)

- A vector instruction performs an operation on each element in consecutive cycles
- Vector functional units are pipelined
- Each pipeline stage operates on a different data element
- Vector instructions allow deeper pipelines
- No intra-vector dependencies $\rightarrow$ no hardware interlocking within a vector
- No control flow within a vector
- Known stride allows prefetching of vectors into cache/memory


## Vector Processor Advantages

+ No dependencies within a vector
- Pipelining, parallelization work well
- Can have very deep pipelines, no dependencies!
+ Each instruction generates a lot of work
- Reduces instruction fetch bandwidth
+ Highly regular memory access pattern
- Interleaving multiple banks for higher memory bandwidth
- Prefetching
+ No need to explicitly code loops
- Fewer branches in the instruction sequence


## Vector Processor Disadvantages

-- Works (only) if parallelism is regular (data/SIMD parallelism) ++ Vector operations
-- Very inefficient if parallelism is irregular -- How about searching for a key in a linked list?

To program a vector machine, the compiler or hand coder must make the data structures in the code fit nearly exactly the regular structure built into the hardware. That's hard to do in first place, and just as hard to change. One tweak, and the low-level code has to be rewritten by a very smart and dedicated programmer who knows the hardware and often the subtleties of the application area. Often the rewriting is

Fisher, "Very Long Instruction Word architectures and the ELI-512," ISCA 1983.

## Vector Processor Limitations

-- Memory (bandwidth) can easily become a bottleneck, especially if

1. compute/memory operation balance is not maintained
2. data is not mapped appropriately to memory banks

We did not cover the following slides in lecture. These are for your preparation for the next lecture.

## Vector Registers

- Each vector data register holds N M-bit values
- Vector control registers: VLEN, VSTR, VMASK
- Vector Mask Register (VMASK)
- Indicates which elements of vector to operate on
- Set by vector test instructions
- e.g., VMASK[i] = (Vk $\left.{ }_{k}[i]==0\right)$
- Maximum VLEN can be N
- Maximum number of elements stored in a vector register



## Vector Functional Units

- Use deep pipeline (=> fast clock) to execute element operations
- Simplifies control of deep pipeline because elements in vector are independent

Six stage multiply pipeline


V3 <- v1 * v2

## Vector Machine Organization (CRAY-1)



- CRAY-1
- Russell, "The CRAY-1 computer system," CACM 1978.
- Scalar and vector modes
- 864-element vector registers
- 64 bits per element
- 16 memory banks
- 8 64-bit scalar registers
- 8 24-bit address registers


## Memory Banking

- Example: 16 banks; can start one bank access per cycle
- Bank latency: 11 cycles
- Can sustain 16 parallel accesses if they go to different banks

| $\begin{aligned} & \text { Bank } \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { Bank } \\ & 1 \end{aligned}$ | $\begin{aligned} & \text { Bank } \\ & 2 \end{aligned}$ |  | $\begin{aligned} & \text { Bank } \\ & 15 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |



## Vector Memory System



## Scalar Code Example

- For $\mathrm{I}=0$ to 49
- $C[i]=(A[i]+B[i]) / 2$
- Scalar code

MOVI R0 $=50 \quad 1$
MOVA R1 $=\mathrm{A}$
MOVA R2 $=B$
MOVA R3 = C
X: LD R4 = MEM[R1++]
LD R5 = MEM[R2++]
ADD R6 = R4 + R5
SHFR R7 = R6 >> 1
ST MEM[R3++] = R7
DECBNZ --R0, X

304 dynamic instructions1

11 ;autoincrement addressing

11
4
1
11
2 ;decrement and branch if NZ

## Scalar Code Execution Time

- Scalar execution time on an in-order processor with 1 bank
- First two loads in the loop cannot be pipelined: 2*11 cycles
- $4+50 * 40=2004$ cycles
- Scalar execution time on an in-order processor with 16 banks (word-interleaved)
- First two loads in the loop can be pipelined
- $4+50 * 30=1504$ cycles
- Why 16 banks?
- 11 cycle memory access latency
- Having 16 (>11) banks ensures there are enough banks to overlap enough memory operations to cover memory latency


## Vectorizable Loops

- A loop is vectorizable if each iteration is independent of any other
- For $\mathrm{I}=0$ to 49
- $C[i]=(A[i]+B[i]) / 2$

7 dynamic instructions

- Vectorized loop:

MOVI VLEN $=50 \quad 1$
MOVI VSTR $=1 \quad 1$
VLD V0 = A
VLD V1 = B
VADD V2 = V0 + V1
VSHFR V3 = V2 >> 1
$11+$ VLN - 1
$11+$ VLN - 1
$4+$ VLN - 1
$1+$ VLN - 1
VST C = V3

## Vector Code Performance

- No chaining
- i.e., output of a vector functional unit cannot be used as the input of another (i.e., no vector data forwarding)
- One memory port (one address generator)
- 16 memory banks (word-interleaved)

- 285 cycles


## Vector Chaining

- Vector chaining: Data forwarding from one vector functional unit to another



## Vector Code Performance - Chaining

- Vector chaining: Data forwarding from one vector functional unit to another



## Vector Code Performance - Multiple Memory Ports

- Chaining and 2 load ports, 1 store port in each bank

- 79 cycles


## Questions (I)

- What if \# data elements > \# elements in a vector register?
- Need to break loops so that each iteration operates on \# elements in a vector register
- E.g., 527 data elements, 64-element VREGs
- 8 iterations where VLEN $=64$
- 1 iteration where VLEN = 15 (need to change value of VLEN)
- Called vector stripmining
- What if vector data is not stored in a strided fashion in memory? (irregular memory access to a vector)
- Use indirection to combine elements into vector registers
- Called scatter/gather operations


## Gather/Scatter Operations

Want to vectorize loops with indirect accesses:

$$
\begin{aligned}
\text { for } & (i=0 ; i<N ; i++) \\
& A[i]=B[i]+C[D[i]]
\end{aligned}
$$

Indexed load instruction (Gather)

```
LV vD, rD # Load indices in D vector
LVI vC, rC, vD # Load indirect from rC base
LV vB, rB # Load B vector
ADDV.D vA,vB,vC # Do add
SV vA, rA
# Store result
```


## Gather/Scatter Operations

- Gather/scatter operations often implemented in hardware to handle sparse matrices
- Vector loads and stores use an index vector which is added to the base register to generate the addresses

Index Vector

| 1 | 3.14 | 3.14 |
| :---: | :---: | :---: |
| 3 | 6.5 | 0.0 |
| 7 | 71.2 | 6.5 |
| 8 | 2.71 | 0.0 |
|  |  | 0.0 |
|  |  | 0.0 |
|  |  | 0.0 |
|  |  | 71.2 |
|  |  | 2.7 |

Equivalent

## Conditional Operations in a Loop

- What if some operations should not be executed on a vector (based on a dynamically-determined condition)? loop:
if $(a[i]!=0)$ then $b[i]=a[i] * b[i]$
goto loop
- Idea: Masked operations
- VMASK register is a bit mask determining which data element should not be acted upon

$$
\begin{aligned}
& \text { VLD V0 }=\mathrm{A} \\
& \text { VLD V1 }=\mathrm{B} \\
& \text { VMASK }=(\mathrm{V} 0!=0) \\
& \text { VMUL V1 }=\text { V } 0 * V 1 \\
& \text { VST } \mathrm{B}=\mathrm{V} 1
\end{aligned}
$$

- Does this look familiar? This is essentially predicated execution.


## Another Example with Masking

$$
\begin{aligned}
& \text { for }(\mathrm{i}=0 ; \mathrm{i}<64 ;++\mathrm{i}) \\
& \quad \text { if }(\mathrm{a}[\mathrm{i}]>=\mathrm{b}[\mathrm{i}]) \text { then } \mathrm{c}[\mathrm{i}]=\mathrm{a}[\mathrm{i}] \\
& \quad \text { else } \mathrm{c}[\mathrm{i}]=\mathrm{b}[\mathrm{i}]
\end{aligned}
$$

| A | B | VMASK |
| :--- | :--- | :---: |
| 1 | 2 | 0 |
| 2 | 2 | 1 |
| 3 | 2 | 1 |
| 4 | 10 | 0 |
| -5 | -4 | 0 |
| 0 | -3 | 1 |
| 6 | 5 | 1 |
| -7 | -8 | 1 |

Steps to execute loop

1. Compare $A, B$ to get VMASK
2. Masked store of $A$ into $C$
3. Complement VMASK
4. Masked store of B into C

## Masked Vector Instructions

## Simple Implementation

- execute all N operations, turn off result writeback according to mask


Density-Time Implementation

- scan mask vector and only execute elements with non-zero masks



## Some Issues

- Stride and banking
- As long as they are relatively prime to each other and there are enough banks to cover bank access latency, consecutive accesses proceed in parallel
- Storage of a matrix
- Row major: Consecutive elements in a row are laid out consecutively in memory
- Column major: Consecutive elements in a column are laid out consecutively in memory
- You need to change the stride when accessing a row versus column

Matrix multiplication
$A$ \& $B$, both in raw major order

AD | 0 |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 1 | 2 | 3 | 4 | 5 |  |
| 6 | 7 | 8 | 9 | 10 | 11 |  |
|  |  |  |  |  |  |  |

$\int^{B_{0}}$| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 |
| 20 |  |  |  |  |  |  |  |  |  |
| 30 |  |  |  |  |  |  |  |  |  |
| 40 |  |  |  |  |  |  |  |  |  |
| 50 |  |  |  |  |  |  |  |  |  |

$A_{4 \times 6} B_{9 \times 10} \rightarrow C_{4 \times 10}$ (dot products of rows \& coins of $A \& B$ )
A: Load $A_{0}$ into a vector register V1
$\rightarrow$ each time you need to moromest the address by 1 to access the nest cetus
$\rightarrow$ First matrix Guesses have 0 stride of 1
B. 4 cad Bointe a vectorvegister $V 2$
$\rightarrow$ econ the yo r reed to molest by 10
$\rightarrow$ stride of 10

Different strides can lead to bonk confleds.
$\rightarrow$ How do you mismate tron?

Array vs. Vector Processors, Revisited

- Array vs. vector processor distinction is a "purist's" distinction
- Most "modern" SIMD processors are a combination of both
- They exploit data parallelism in both time and space


## Remember: Array vs. Vector Processors



Instruction Stream
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Same op @ same time

| LD0 | LD1 | LD2 | LD3 |
| :--- | :--- | :--- | :--- |
| AD0 | AD1 | AD2 | AD3 |
| MU0 | MU1 | MU2 | MU3 |
| ST0 | ST1 | ST2 | ST3 |

Different ops @ same space

| Different ops @ time |  |  |  |
| :---: | :---: | :---: | :---: |
| L1 |  |  |  |
| LD2 | AD1 | MU0 |  |
| LD3 | AD2 | MU1 | STO |
|  | AD3 | MU2 | ST1 |
|  |  | MU3 | ST2 |
| Same op @ space ST3 |  |  |  |



## Vector Instruction Execution



## Vector Unit Structure



## Vector Instruction Level Parallelism

Can overlap execution of multiple vector instructions

- example machine has 32 elements per vector register and 8 lanes
- Complete 24 operations/cycle while issuing 1 short instruction/cycle



## Automatic Code Vectorization

$$
\begin{aligned}
\text { for } & (i=0 ; i<N ; i++) \\
& C[i]=A[i]+B[i] ;
\end{aligned}
$$

Scalar Sequential Code

Vectorized Code


Vectorization is a compile-time reordering of operation sequencing
$\Rightarrow$ requires extensive loop dependence analysis

## Vector/SIMD Processing Summary

- Vector/SIMD machines good at exploiting regular data-level parallelism
- Same operation performed on many data elements
- Improve performance, simplify design (no intra-vector dependencies)
- Performance improvement limited by vectorizability of code
- Scalar operations limit vector machine performance
- Amdahl's Law
- CRAY-1 was the fastest SCALAR machine at its time!
- Many existing ISAs include (vector-like) SIMD operations
- Intel MMX/SSEn/AVX, PowerPC AltiVec, ARM Advanced SIMD


## SIMD Operations in Modern ISAs

## Intel Pentium MMX Operations

- Idea: One instruction operates on multiple data elements simultaneously
- Ala array processing (yet much more limited)
- Designed with multimedia (graphics) operations in mind


Figure 1. MMX technology data types: packed byte (a), packed word (b), packed doubleword (c), and quadword (d).

No VLEN register
Opcode determines data type:
8 8-bit bytes
4 16-bit words
2 32-bit doublewords
1 64-bit quadword

Stride always equal to 1.

Peleg and Weiser, "MMX Technology Extension to the Intel Architecture," IEEE Micro, 1996.

## MMX Example: Image Overlaying (I)


$=$


Figure 8. Chroma keying: image overlay using a background color.

## PCMPEQB MM1, MM3



Bitmask

Figure 9. Generating the selection bit mask.

## MMX Example: Image Overlaying (II)

PAND MM4, MM1


MM1 | $0 \times 0000$ | $0 \times 0000$ | $0 \times F F F F$ | $0 \times F F F F$ | $0 \times 0000$ | $0 \times 0000$ | $0 \times F F F F$ | $0 \times F F F F$ | MM3 | $\mathrm{X}_{7}$ | $\mathrm{X}_{6}$ | $\mathrm{X}_{5}$ | $\mathrm{X}_{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |




Figure 10. Using the mask with logical MMX instructions to perform a conditional select.

| Mova | mm3, mem1 | /* Load eight pixels from woman's image |
| :---: | :---: | :---: |
| Movq | mm 4 , mem2 | 7 Load eight pixels from the blossom image |
| Pcmpeqb | $\mathrm{mm1}, \mathrm{mm3}$ |  |
| Pand | mm4, mm1 |  |
| Pandn | $\mathrm{mm} 1, \mathrm{~mm} 3$ |  |
| Por | mm4, mm1 |  |

Figure 11. MMX code sequence for performing a conditional select.

