

18734: Foundations of Privacy

Policy Auditing over Incomplete Logs:  
The reduce algorithm

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# Example from HIPAA Privacy Rule

A covered entity may disclose an individual's protected health information (phi) to law-enforcement officials for the purpose of identifying an individual if the individual made a statement admitting participating in a violent crime that the covered entity believes may have caused serious physical harm to the victim

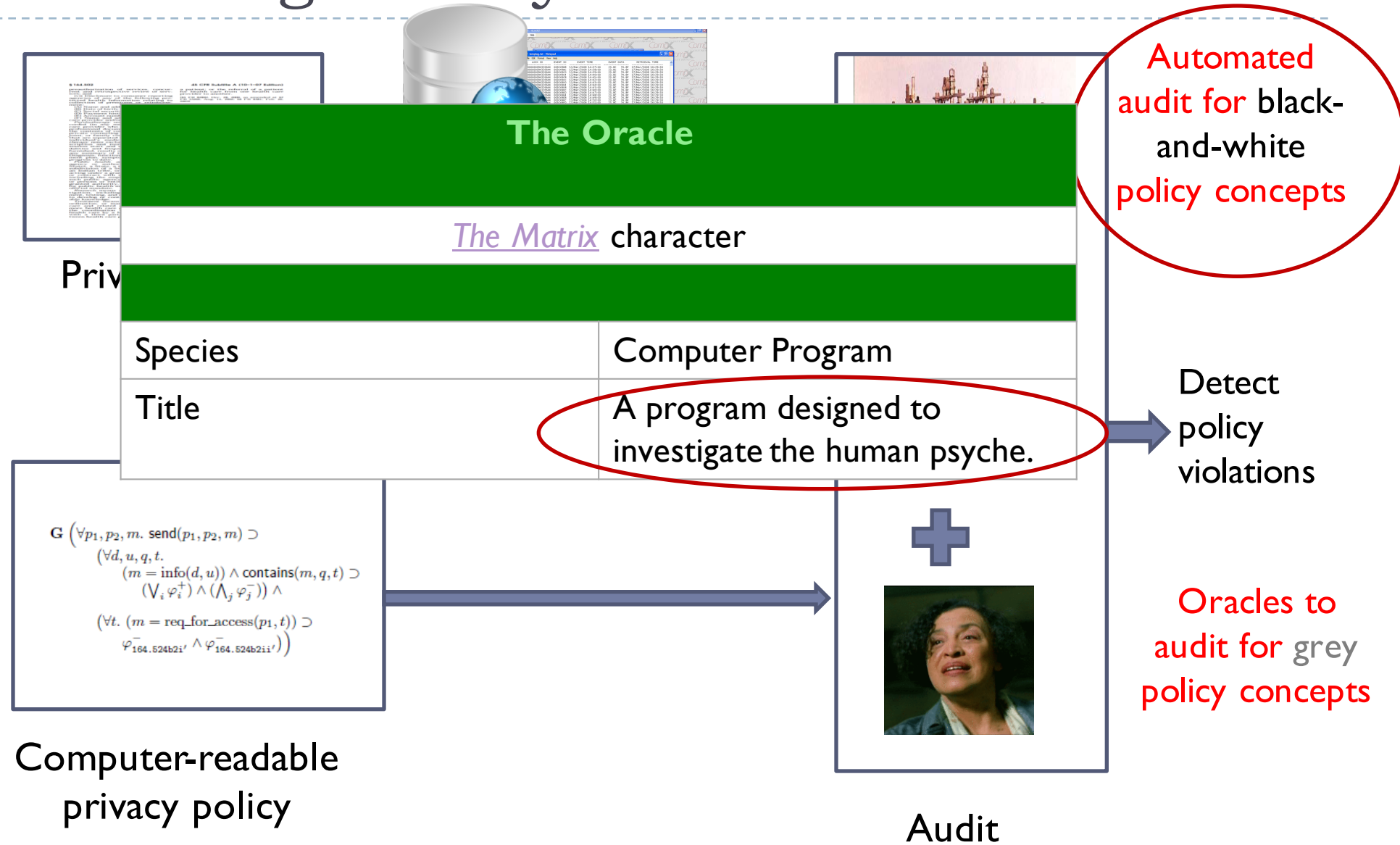
## ▶ Concepts in privacy policies

- ▶ **Actions:** send(p1, p2, m)
- ▶ **Roles:** inrole(p2, law-enforcement)
- ▶ **Data attributes:** attr\_in(prescription, phi)
- ▶ **Temporal constraints:** in-the-past(state(q, m))
  
- ▶ **Purposes:** purp\_in(u, id-criminal))
- ▶ **Beliefs:** believes-crime-caused-serious-harm(p, q, m)

Black-and-white concepts

Grey concepts

# Detecting Privacy Violations



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# Auditing Black-and-White Policy Concepts

With D. Garg (CMU → MPI-SWS) and L. Jia (CMU)

2011 ACM Conference on Computer and  
Communications Security

# Key Challenge for Auditing

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## Audit Logs are Incomplete

**Future: store only past and current events**

Example: Timely data breach notification refers to future event

**Subjective: no “grey” information**

Example: May not record evidence for purposes and beliefs

**Spatial: remote logs may be inaccessible**

Example: Logs distributed across different departments of a hospital

# Abstract Model of Incomplete Logs

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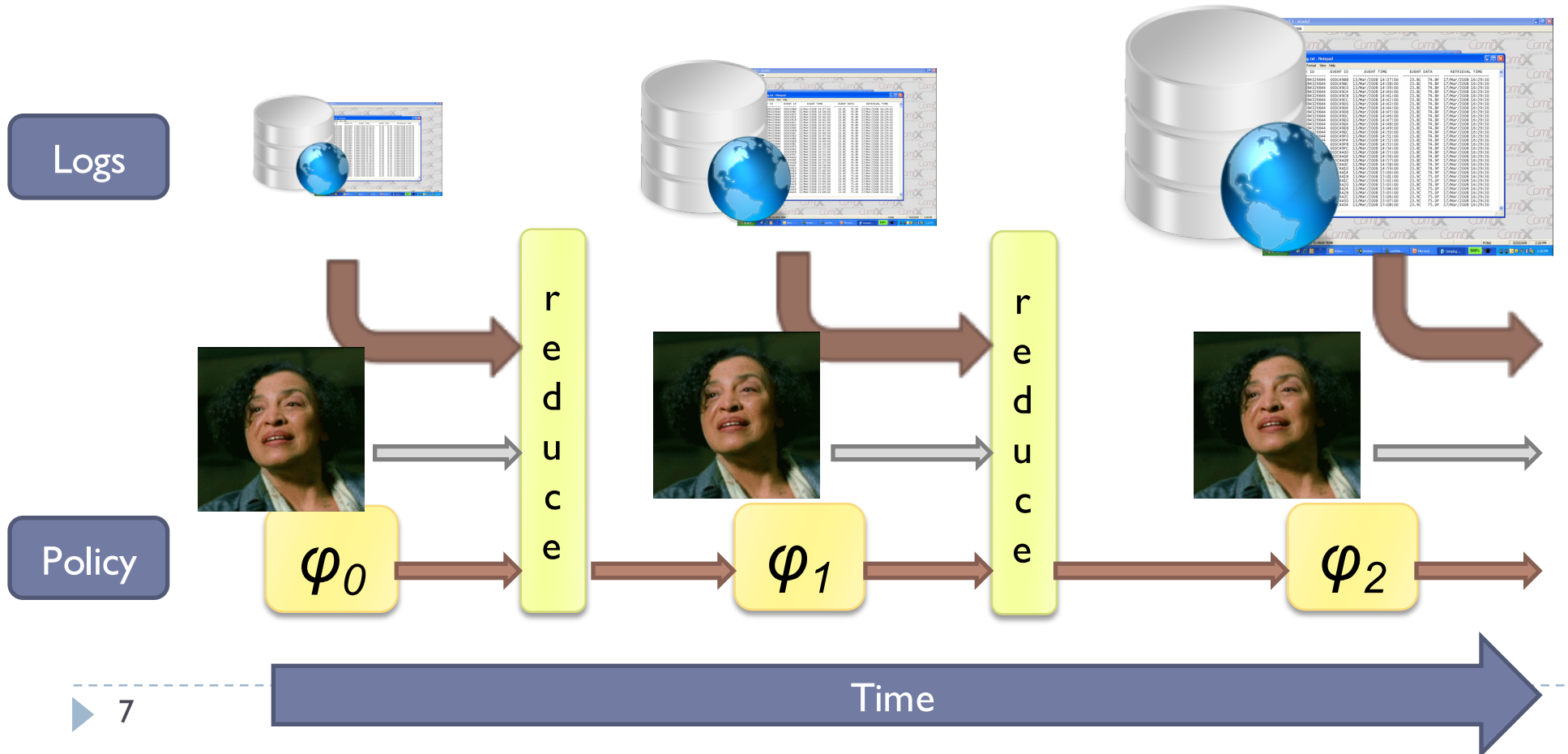
Model **all** incomplete logs uniformly as **3-valued structures**

$$\mathcal{L}(P) \in \{tt, ff, uu\}$$

Define **semantics** (meanings of formulas) over 3-valued structures

# reduce: The Iterative Algorithm

$$\text{reduce}(\mathcal{L}, \varphi) = \varphi'$$



# Syntax of Policy Logic

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Atoms	$P$	$::=$	$p(t_1, \dots, t_n)$
Formulas	$\varphi$	$::=$	$P \mid \top \mid \perp \mid$ $\varphi_1 \wedge \varphi_2 \mid \varphi_1 \vee \varphi_2 \mid$ $\forall \vec{x}.(c \supset \varphi) \mid \exists \vec{x}.(c \wedge \varphi)$
Restrictions	$c$	$::=$	$P \mid \top \mid \perp \mid c_1 \wedge c_2 \mid$ $c_1 \vee c_2 \mid \exists x.c$

- ▶ First-order logic with restricted quantification over *infinite domains* (challenge for reduce)
- ▶ Can express timed temporal properties, “grey” predicates



# Example from HIPAA Privacy Rule

A covered entity may disclose an individual's protected health information (phi) to law-enforcement officials for the purpose of identifying an individual if the individual made a statement admitting participating in a violent crime that the covered entity believes may have caused serious physical harm to the victim

$$\begin{aligned} & \forall p1, p2, m, u, q, t. \\ & (\text{send}(p1, p2, m) \wedge \\ & \text{tagged}(m, q, t, u) \wedge \\ & \text{attr\_in}(t, \text{phi})) \\ & \supset \text{inrole}(p1, \text{covered-entity}) \wedge \text{inrole}(p2, \text{law-enforcement}) \\ & (\text{purp\_in}(u, \text{id-criminal})) \wedge \\ & \wedge \exists m' \diamond \text{state}(q, m') \wedge \text{is-admission-of-crime}(m') \\ & \wedge \text{believes-crime-caused-serious-harm}(p1, q, m') \end{aligned}$$

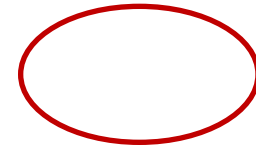
# reduce: Formal Definition

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$(\top \text{ if } \rho(P) = \top\top$

General Theorem: If initial policy passes a syntactic **mode check**, then finite substitutions can be computed

$\text{reduce}(L, \forall x.\varphi)$



c is a finite substitution

Applications: The entire HIPAA and GLBA Privacy Rules pass this check

# Example

$\varphi =$

$\forall p1, p2, m, u, q, t.$

$(\text{send}(p1, p2, m) \wedge$   
 $\text{tagged}(m, q, t, u) \wedge$   
 $\text{attr\_in}(t, \text{phi}))$

$\wedge \text{inrole}(p1, \text{covered-entity}) \wedge \text{inrole}(p2, \text{law-enforcement})$

$\wedge \text{purp\_in}(u, \text{id-criminal})$

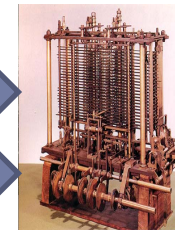
$\wedge \exists m'. (\text{state}(q, m')$

$\wedge \text{is-admission-of-crime}(m')$

$\wedge \text{believes-crime-caused-serious-harm}(p1, m')$

$\{ p1 \rightarrow \text{UPMC},$   
 $p2 \rightarrow \text{allegeny-police},$   
 $m \rightarrow \text{M2},$   
 $q \rightarrow \text{Bob},$   
 $u \rightarrow \text{id-bank-robber},$   
 $t \rightarrow \text{date-of-treatment}$   
 $\}$

$\{ m' \rightarrow \text{M1} \}$



## Log

Aug 15, 2014

$\text{state}(\text{Bob}, \text{M1})$

Sept 17, 2014

$\text{send}(\text{UPMC}, \text{allegeny-police}, \text{M2})$   
 $\text{tagged}(\text{M2}, \text{Bob}, \text{date-of-treatment},$   
 $\text{id-bank-robber})$

$\varphi' = \top$

$\wedge \text{purp\_in}(\text{id-bank-robber}, \text{id-criminal})$

$\wedge \text{is-admission-of-crime}(\text{M1})$

$\wedge \text{believes-crime-caused-serious-harm}(\text{UPMC}, \text{M1})$



# Correctness of Reduce

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**Theorem 3.2** (Partial correctness of reduce). *If  $\text{reduce}(\mathcal{L}, \varphi) = \psi$  and  $\mathcal{L} \leq \mathcal{L}'$ , then (1)  $\mathcal{L}' \models \varphi$  iff  $\mathcal{L}' \models \psi$  and (2)  $\mathcal{L}' \models \bar{\varphi}$  iff  $\mathcal{L}' \models \bar{\psi}$ .*

# Implementation and Case Study

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- ▶ Implementation and evaluation over simulated audit logs for compliance with *all* 84 disclosure-related clauses of HIPAA Privacy Rule
- ▶ Performance:
  - ▶ Average time for checking compliance of each disclosure of protected health information is 0.12s for a 15MB log
- ▶ Mechanical enforcement:
  - ▶ reduce can automatically check 80% of all the atomic predicates

# Ongoing Transition Efforts

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- ▶ Integration of reduce algorithm into Illinois Health Information Exchange prototype
  - ▶ Joint work with UIUC and Illinois HLN
  
- ▶ Auditing logs for policy compliance
  - ▶ Ongoing conversations with Symantec Research

# Applications of Reduce

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- ▶ Audit to detect violations of policy or demonstrate compliance
- ▶ Provide explanations for violations (e.g., which clause of HIPAA was violated)
- ▶ Help train employees about privacy laws (e.g., check whether a certain type of disclosure is permitted by HIPAA)

# Learning Outcomes for You

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- ▶ Translate privacy laws into first-order logic for use by reduce
- ▶ Use reduce tool to check logs for compliance with laws
- ▶ Use reduce to check whether certain types of disclosures are permitted by a privacy law

Homework I will make you work through these problems  
Possible project around other privacy laws such as FERPA,  
COPPA



# Related Work

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## Privacy Specification Languages

- P3P[Cranor et al.], XACML[OASIS], EPAL[Backes et al.]:  
Less expressive (no temporal ops,..)
- *Logic of Privacy and Utility* [Barth et al]:  
Related specification logic;  
enforcement only for propositional  
fragment

# Related Work

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## Logical Specification of Privacy Laws

Smaller fragments of laws

- *Logic of Privacy and Utility* [Barth et al.]: Example clauses from HIPAA and GLBA
- PrivacyAPIs [Gunter et al.]: HIPAA 164.506
- Datalog HIPAA [Lam et al.]: HIPAA 164.502, 164.506, 164.510

## Related Work

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### **Runtime monitoring in MFOTL**

[Basin et al '10]

- Pre-emptive enforcement
- Efficient implementation
- Assumes past-completeness of logs
- Less expressive mode checking (“safe-range check”)
- Cannot express HIPAA or GLBA

# Related Work

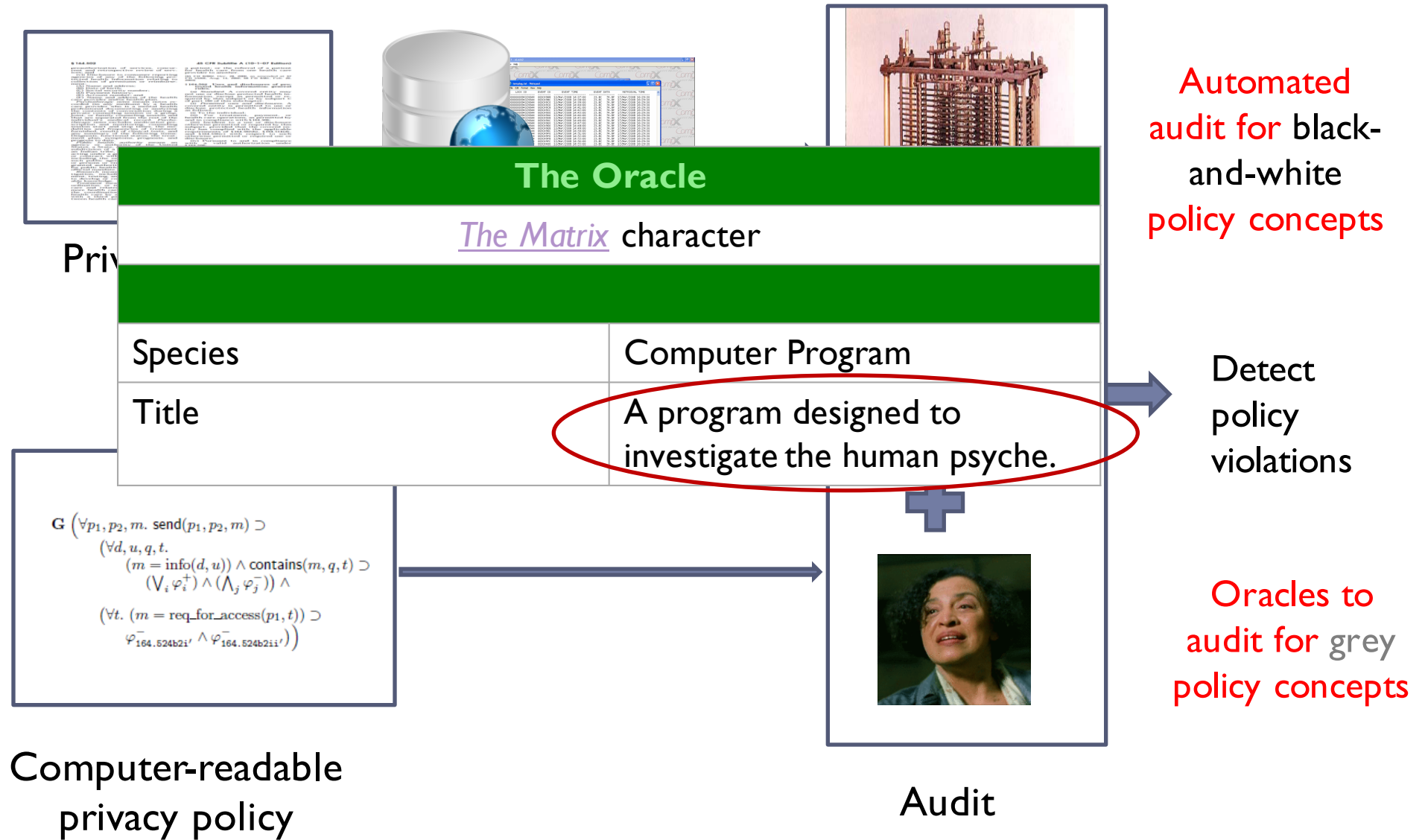
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## **Industry practice**

### Fairwarning Audit Tool

- Customized SQL queries over access logs
- Queries not tied to policy clauses

# Detecting Policy Violations



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Thanks!

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# More Technical Details

# Definition of $\widehat{\text{sat}}$

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Assume: The function  $\text{sat}(L, P)$  computes all substitutions  $\sigma$  for variables in  $P$  such that  $L \models P\sigma$ , if certain argument positions in  $P$  are ground.

$$\begin{aligned}\widehat{\text{sat}}(L, p_O(t_1, \dots, t_n)) &= \text{sat}(L, p_O(t_1, \dots, t_n)) \\ \widehat{\text{sat}}(L, \top) &= \{\bullet\} \\ \widehat{\text{sat}}(L, \perp) &= \{\} \\ \widehat{\text{sat}}(L, c_1 \wedge c_2) &= \bigcup_{\sigma \in \widehat{\text{sat}}(L, c_1)} \sigma + \widehat{\text{sat}}(L, c_2\sigma) \\ \widehat{\text{sat}}(L, c_1 \vee c_2) &= \widehat{\text{sat}}(L, c_1) \cup \widehat{\text{sat}}(L, c_2) \\ \widehat{\text{sat}}(L, \exists x.c) &= \widehat{\text{sat}}(L, c) \setminus \{x\} \quad (x \text{ fresh})\end{aligned}$$



# Mode Analysis: Idea

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- ▶ Example 1:  $\text{address}(x, y, a) = x + y < a$
- ▶ Key idea: If input positions are grounded, then only finite number of satisfying substitutions for output positions.
- ▶ Example 1 moding:  $\text{address}(+, -, +)$
- ▶ Example 2:  $\theta = \text{send}(p1, p2, m) \wedge \text{tagged}(m, q, t, u)$
- ▶  $\text{send}(-, -, -)$ : all positions are output mode
- ▶  $\text{tagged}(+, -, -, -)$ : message position is input mode

# Mode Analysis: Predicates

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$$\boxed{\chi_I \vdash c : \chi_O}$$

1.  $\{\} \vdash \text{send}(p_1, p_2, m) : \{p_1, p_2, m\}$
2.  $\{p_1, p_2, m\} \vdash \text{tagged}(m, q, t, u) : \{p_1, p_2, m, q, t, u\}$

$$\frac{\forall k \in I(p_O). \text{fv}(t_k) \subseteq \chi_I \quad \chi_O = \chi_I \cup \left( \bigcup_{j \in O(p_O)} \text{fv}(t_j) \right)}{\chi_I \vdash p_O(t_1, \dots, t_n) : \chi_O}$$

# Mode Analysis: Conjunction

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1.  $\{\} \vdash \text{send}(p1, p2, m) : \{p1, p2, m\}$
2.  $\{p1, p2, m\} \vdash \text{tagged}(m, q, t, u) : \{p1, p2, m, q, t, u\}$
3.  $\{\} \vdash \text{send}(p1, p2, m) \wedge \text{tagged}(m, q, t, u) : \{p1, p2, m, q, t, u\}$

$$\frac{\chi_I \vdash c_1 : \chi \quad \chi \vdash c_2 : \chi_O}{\chi_I \vdash c_1 \wedge c_2 : \chi_O}$$

# Mode Analysis and $\widehat{\text{sat}}$

Example:  $\theta = \text{send}(p1, p2, m) \wedge \text{tagged}(m, q, t, u)$

- ▶  $\text{send}(-,-,-)$ : all positions are output mode
- ▶  $\text{tagged}(+,-,-,-)$ : message position is input mode
- ▶  $\widehat{\text{sat}}(\theta) = \text{sat}(\text{send}(p1, p2, m)) + \text{sat}(\text{tagged}(m, q, t, u) \sigma)$

$\sigma$

{ p1 → UPMC,  
p2 → allegeny-police,  
m → M2,  
q → Bob,  
u → id-bank-robber,  
t → date-of-treatment

## Log

Jan 1, 2011  
state(Bob, M1)

Jan 5, 2011  
send(UPMC, allegeny-police, M2)  
tagged(M2, Bob, date-of-treatment,  
id-bank-robber)

# Mode Analysis: Termination of $\widehat{\text{sat}}$

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General Theorem: If initial policy passes a syntactic **mode check**, then finite substitutions can be computed

Applications: The entire HIPAA and GLBA Privacy Rules pass this check