

18734 Recitation

Distance Metrics

October 6, 2017

	Non-Sensitive			Sensitive
	Zip Code	Age	Nationality	Condition
1	13053	28	Russian	Heart Disease
2	13068	29	American	Heart Disease
3	13068	21	Japanese	Viral Infection
4	13053	23	American	Viral Infection
5	14853	50	Indian	Cancer
6	14853	55	Russian	Heart Disease
7	14850	47	American	Viral Infection
8	14850	49	American	Viral Infection
9	13053	31	American	Cancer
10	13053	37	Indian	Cancer
11	13068	36	Japanese	Cancer
12	13068	35	American	Cancer

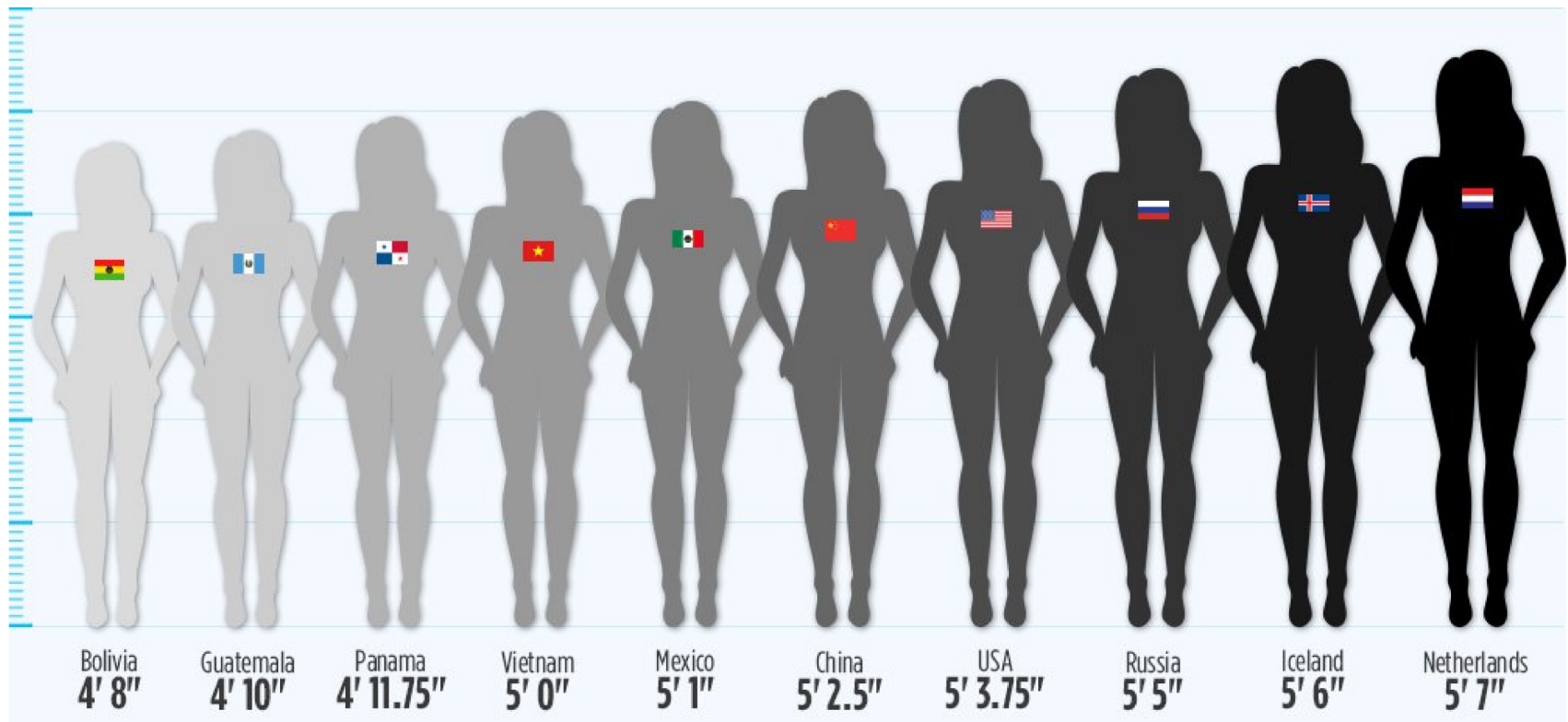
Figure 1. Inpatient Microdata

	Non-Sensitive			Sensitive
	Zip Code	Age	Nationality	Condition
1	130**	< 30	*	Heart Disease
2	130**	< 30	*	Heart Disease
3	130**	< 30	*	Viral Infection
4	130**	< 30	*	Viral Infection
5	1485*	≥ 40	*	Cancer
6	1485*	≥ 40	*	Heart Disease
7	1485*	≥ 40	*	Viral Infection
8	1485*	≥ 40	*	Viral Infection
9	130**	3*	*	Cancer
10	130**	3*	*	Cancer
11	130**	3*	*	Cancer
12	130**	3*	*	Cancer

Figure 2. 4-anonymous Inpatient Microdata

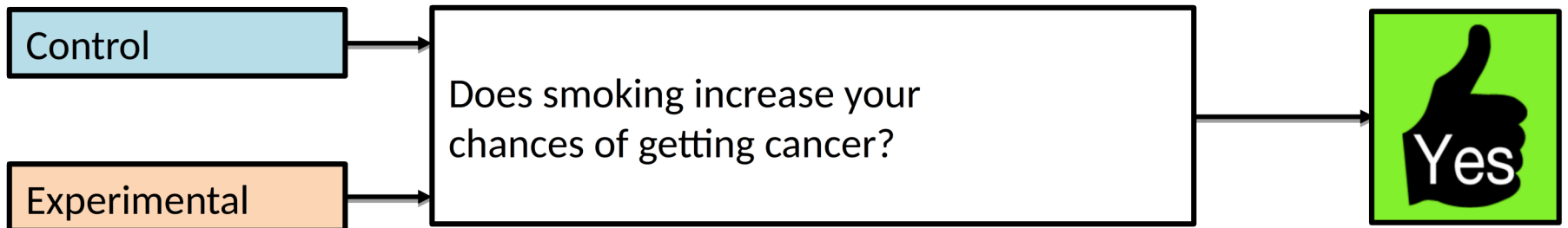
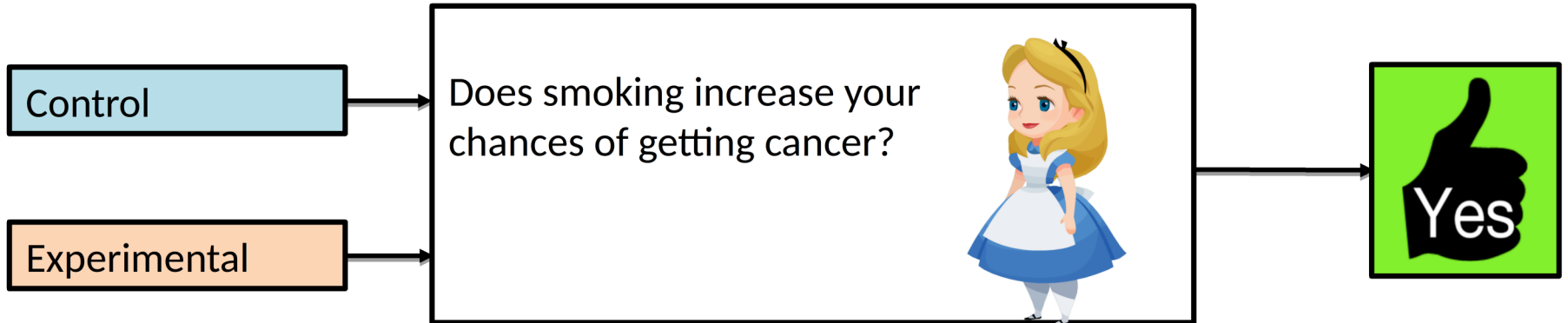
Goal of Statistical Disclosure Control

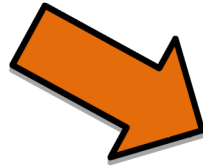
Reveal accurate statistics about a population while preserving the privacy of individuals



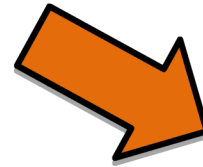
Stephanie Sun is one inch shorter than the average Russian woman

Differential Privacy

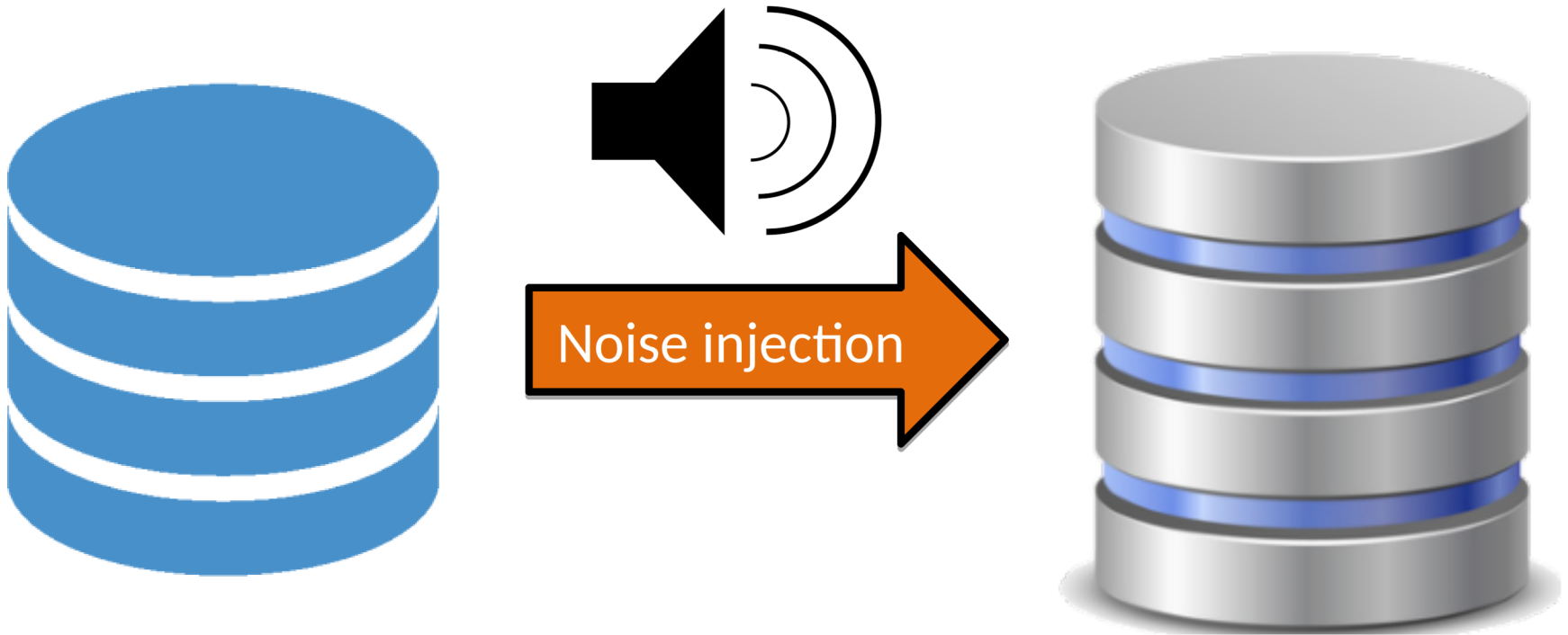




Study



Input perturbation

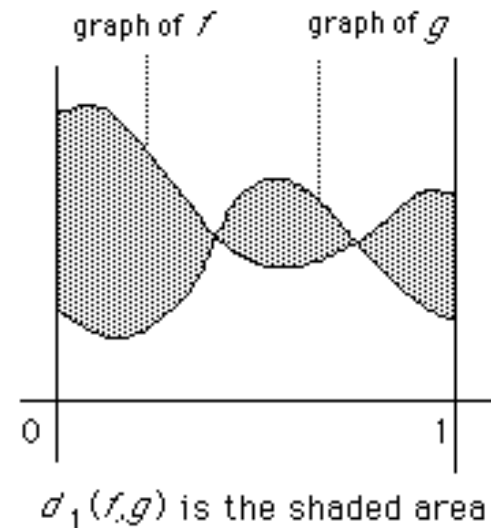


L1 Distance

- Between two points
 - (x_1, x_2, \dots, x_n) and (y_1, y_2, \dots, y_n)
- $\sum_i |x_i - y_i|$

Distance between functions

- Between two discrete functions
 - $m_1(x), m_2(x)$
 - $x \in \{x_1, x_2, \dots, x_n\}$
 - $\sum_i |m_1(x_i) - m_2(x_i)|$
- Between two continuous functions
 - $n_1(y), n_2(y)$
 - $y \in [y_1, y_2]$
 - $\int_{y_1}^{y_2} |n_1(y) - n_2(y)| dy$



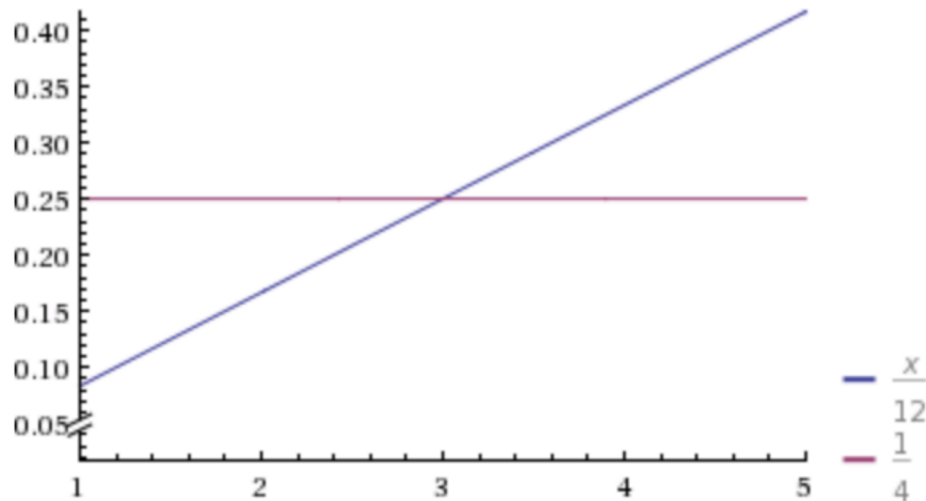
Distance between probability distributions

- Between two discrete distributions
 - PMFs $p_1(x)$, $p_2(x)$
 - $x \in \{x_1, x_2, \dots, x_n\}$
 - $\sum_i |p_1(x_i) - p_2(x_i)|$
- Between two continuous distributions
 - PDFs $f_1(y)$, $f_2(y)$
 - $y \in [y_1, y_2]$
 - $\int_{y_1}^{y_2} |f_1(y) - f_2(y)| dy$

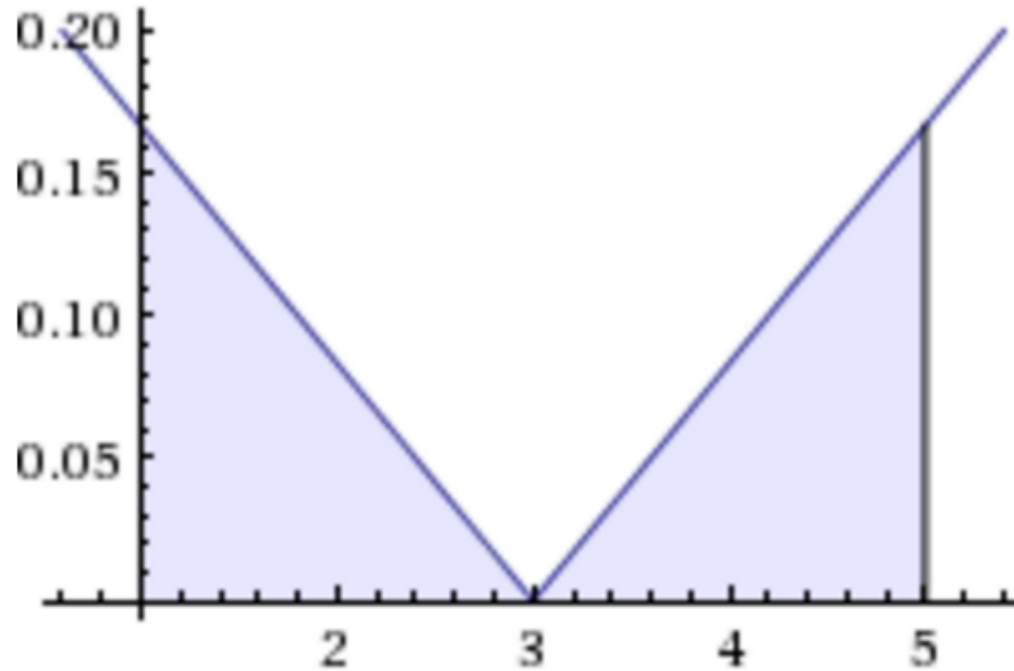
Exercise

- Find L1 distance between the following continuous distributions:
 - $f_1(x) = x/12 \quad x \in [1, 5]$
 - $f_2(x) = 1/4 \quad x \in [1, 5]$

Plot:



Solution: $1/3$



Individual Fairness

Treat *similar* individuals *similarly*



Similar for the purpose of
the classification task

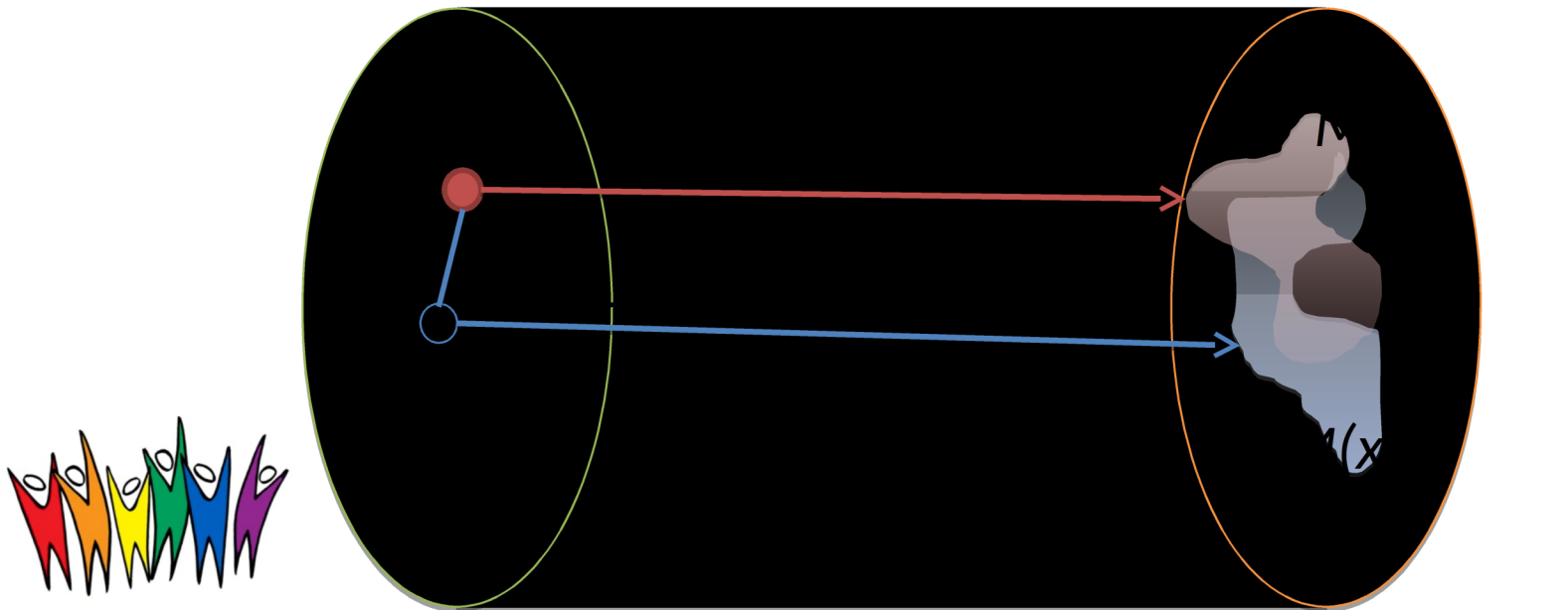


Similar distribution
over outcomes

Fairness through Awareness

Metric $d: V \times V \rightarrow \mathbb{R}$

Lipschitz condition $\|M(x) - M(y)\| \leq d(x, y)$



V: Individuals

O: outcomes

Statistical Distance

- P, Q are probability measures on a finite domain A.
- Statistical distance between P and Q is:

$$- D(P, Q) = \frac{1}{2} \sum_{a \in A} |P(a) - Q(a)|$$

- where $M(x)=P, M(y)=Q, O=A$

Example: Mid D

$$A = \{0, 1\}$$





$$P(0) = P(1) = \frac{1}{2}$$

$$Q(0) = \frac{3}{4}, Q(1) = \frac{1}{4}$$

$$D(P, Q) = \frac{1}{4}$$

Installing and Running AdFisher

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Setting up the environment

- AdFisher has been tested on Ubuntu 16.04 with Firefox 45.
- Use a VM if you are running Windows or Mac)
 - <https://www.virtualbox.org/wiki/Downloads>
- Ubuntu
 - <https://www.ubuntu.com/download/desktop>

Downgrade Firefox to Version 45

```
firefox --version Mozilla Firefox 47.0
```

```
apt-get remove firefox
```

```
wget https://
```

```
ftp.mozilla.org/pub/firefox/releases/45.0/linux-x86\_64/en-US/firefox-45.0.tar.bz2
```

```
tar -xjf firefox-45.0.tar.bz2
```

```
mv firefox /opt/firefox45
```

```
ln -s /opt/firefox45/firefox /usr/bin/firefox firefox  
--version Mozilla Firefox 45.0
```

Reference: <http://>

stackoverflow.com/questions/37761668/cant-open-browser-with-selenium-after-firefox-upd

etc

Installing the AdFisher

- Clone the git repository
 - [https://
github.com/tadatitam/info-flow-experiments](https://github.com/tadatitam/info-flow-experiments)
- Follow the instructions to install the python packages AdFisher uses:
 - [https://
github.com/tadatitam/info-flow-experiments/tree
/master/AdFisher](https://github.com/tadatitam/info-flow-experiments/tree/master/AdFisher)

Testing AdFisher

- Cd into AdFisher/examples
- Run **python demo_exp.py**